

Analytic Geometry

January 14, 2016

Proving Theorems About Angles in Parallel Lines Cut by Transversals

EQ: How do angle relationships work together in a set of parallel lines intersected by a transversal?

MCC9-12.G.CO.9 Prove theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints.

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HOMWORK ANSWERS:

1.  $\angle AFD$  and  $\angle DFE$ ;  $\angle BDE$  and  $\angle FDE$

2.  $\angle ACF$  and  $\angle CAF$ ;  $\angle DAF$  and  $\angle DFA$ ;  $\angle DFE$  and  $\angle DBE$   
 $\angle FAD$  and  $\angle ABF$

3.  $\angle AFC$  and  $\angle AFE$ ;  $\angle FDA$  and  $\angle FDB$

4.  $\angle CFA$  and  $\angle ADF$  or  $\angle FDB$ ;  $\angle AFE$  and  $\angle ADF$  or  $\angle FDB$

5.  $90^\circ$ 

6.  $45^\circ$

7.  $135^\circ$

8.  $35^\circ$

9.  $155^\circ$ 

10.  $25^\circ$

11.  $120^\circ$

12.  $60^\circ$

13.  $85^\circ$ 

14.  $60^\circ$  and  $120^\circ$

15.  $32^\circ$  and  $58^\circ$

16.  $69^\circ$  and  $111^\circ$ 

17.  $72^\circ$  and  $108^\circ$

18.  $127^\circ$

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Warm-up:

City planners use geometry when building roads. Below is a portion of a city street map. In the diagram,  $\triangle BAE \sim \triangle CAF$ . Use what you know about similar triangles and angle relationships to answer the questions that follow.

1) If  $m\angle 8 = 30$  and  $m\angle 7 = 80$ , find  $m\angle 2$ .  
Justify your reasoning.

By the third angle theorem,  $\angle 2 = 70$

2) Using the angle measures from problem 1, find the rest of the angle measures and state what angle relationship you used to find each angle measure. Use the following table to help organize the information.

Angle	Measure	Angle relationship used to determine measure
1	110	$\angle 1$ and $\angle 2$ form a linear pair $= 180$
2	70	Third angle theorem
3	110	$\angle 1$ and $\angle 3$ are vertical angles, congruent

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Key Concepts:

A transversal is a line that intersects two or more lines. In the following diagram, line k is the transversal.

The interior angles lie between the parallel lines.

The interior angles are:  $\angle 3, \angle 4, \angle 5,$  and  $\angle 6$ .

The exterior angles lie outside the pair of parallel lines. The exterior angles are:  $\angle 1, \angle 2, \angle 7,$  and  $\angle 8$ .

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Congruent Angles

Angles in the same relative position with respect to the transversal and the intersecting lines are corresponding angles

If the lines that the transversal intersects are parallel, then corresponding angles are congruent.

The corresponding angles are  $\angle 1$  and  $\angle 5$ ;  $\angle 2$  and  $\angle 6$ ;  $\angle 3$  and  $\angle 7$ ;  $\angle 4$  and  $\angle 8$

Alternate Interior angles are angles that are on opposite sides of the transversal and lie on the interior of the two lines that the transversal intersects.

If the two lines that the transversal intersects are parallel, then alternate interior angles are congruent.

The alternate interior angles are  $\angle 3$  and  $\angle 6$ ;  $\angle 4$  and  $\angle 5$

Alternate Exterior angles are angles that are on opposite sides of the transversal and lie on the exterior (outside) of the two lines that the transversal intersects.

If the two lines that the transversal intersects are parallel, then alternate exterior angles are congruent.

The alternate exterior angles are

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Supplementary Angles

in parallel lines

\_\_\_\_\_, also called \_\_\_\_\_, are angles that lie on the same side of the transversal and are in between the lines that the transversal intersects.

If the lines that the transversal intersects are parallel, then same-side interior angles are \_\_\_\_\_.

The consecutive interior angles are \_\_\_\_\_.

\_\_\_\_\_, also called \_\_\_\_\_, are angles that lie on the same side of the transversal and are outside the lines that the transversal intersects.

If the lines that the transversal intersects are parallel, then same-side exterior angles are \_\_\_\_\_.

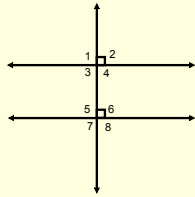
The consecutive exterior angles are \_\_\_\_\_.

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## Special Case!

When the lines that the transversal intersects are parallel and perpendicular to the transversal, then all the interior and exterior angles are

\_\_\_\_\_.

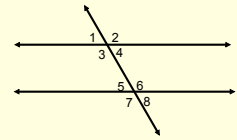


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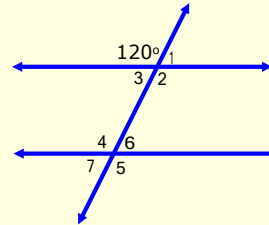
### EXAMPLES:

Name the relationship between the two angles.

1.  $\angle 2$  and  $\angle 7$  alternate exterior
2.  $\angle 2$  and  $\angle 8$  consecutive exterior
3.  $\angle 1$  and  $\angle 5$  corresponding
4.  $\angle 5$  and  $\angle 4$  alternate interior
5.  $\angle 3$  and  $\angle 5$  consecutive interior



6. Find the measures of all the missing angles.

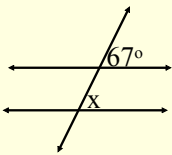


- $\angle 1 = 60^\circ$   
 $\angle 2 = 120^\circ$   
 $\angle 3 = 60^\circ$   
 $\angle 4 = 120^\circ$   
 $\angle 5 = 120^\circ$   
 $\angle 6 = 60^\circ$   
 $\angle 7 = 60^\circ$

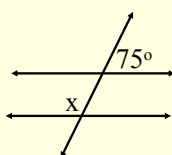
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Identify the angle relationship (if there is one) and then find the value of  $x$  if the lines are parallel.

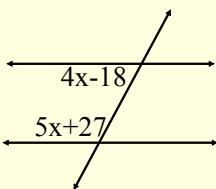
7.  $x = 67$



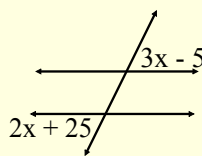
8.  $x = 105$



9.  $x = 19$



10.  $x = 30$

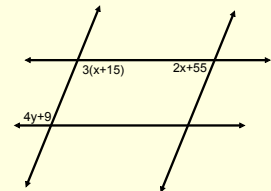


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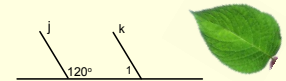
11. Find  $x$  and  $y$ .

$x = 16$

$y = 20.5$



12. Some plants are classified by the arrangement of the veins in their leaves. In the diagram  $j \parallel k$ . What is the  $m\angle 1$ ?



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## HOMEWORK: worksheet

On-line and textbook help references: pp. 67, 72-76  
 - <http://www.mathsisfun.com/geometry/parallel-lines.html>  
 - <http://www.regentsprep.org/Regents/math/geometry/GP8/Lparallel.htm>  
 - <http://www.khanacademy.org/math/basic-geo/basic-geo-angles/basic-geo-angle-relationships/v/angles-formed-by-parallel-lines-and-transversals>

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