

2/11/16

Review for Proofs Quiz

EQ:Name some of the most common properties, theorems, and postulates used when performing proofs.

MCC9-12.G.CO.9 Prove theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints.

MCC9-12.G.CO.10 Prove theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point

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Analytic Geometry Homework: Proofs Answers

Two Column Proof - Complete the proof by filling in the blanks.

Given: $KH \cong KJ$, KM bisects HJ
 Prove: $\angle H \cong \angle J$

| STATEMENTS | REASONS |
|--|---|
| 1) KM bisects HJ | 1) Given |
| 2) $HM \cong JM$ | 2) Definition of bisector |
| 3) $KH \cong KM$ | 3) Given |
| 4) $KM \cong KM$ | 4) Reflexive Property |
| 5) $\triangle KHM \cong \triangle KJM$ | 5) SSS |
| 6) $\angle H \cong \angle J$ | 6) Corresponding parts of \cong triangles are \cong |

Paragraph Proof - Complete the following proof by filling in the blanks.

Given: $\triangle ABC$ with right angle C
 Prove: $\angle A$ and $\angle B$ are complimentary

Proof: $m\angle A + m\angle B + m\angle C = 180$ by the **Triangle Angle Sum Theorem**. It is given that $m\angle C = 90^\circ$, so $m\angle A + m\angle B + 90 = 180$. By Subtraction Property of Equality $m\angle A + m\angle B = 90^\circ$. Thus $\angle A$ and $\angle B$ are complimentary by the definition of complimentary angles.

Flow Proof - Complete the proof by filling in the blanks.

Given: $\angle 1 \cong \angle 7$
 Prove: $l \parallel m$

$\angle 1 \cong \angle 7$

\implies

$\angle 3 \cong \angle 7$

\implies

$l \parallel m$

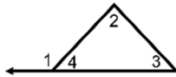
Given
Transitive Property
Corresponding Angles

Vertical Angles are congruent

Complete the proof by filling in the blanks.

Given: $\angle 1$ is an exterior angle of the triangle

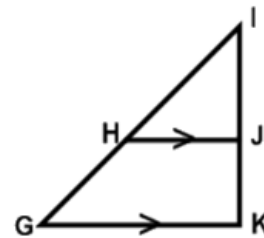
Prove: $m\angle 1 = m\angle 2 + m\angle 3$



| STATEMENTS | REASONS |
|--|---|
| 1) $\angle 1$ is an exterior angle of the triangle | 1) Given |
| 2) $\angle 1$ and $\angle 4$ are supplementary | 2) linear angles are supplementary |
| 3) $m\angle 1 + m\angle 4 = 180$ | 3) Definition of Supplementary |
| 4) $m\angle 2 + m\angle 3 + m\angle 4 = 180$ | 4) Triangle Angle Sum Theorem |
| 5) $m\angle 1 + m\angle 4 = m\angle 2 + m\angle 3 + m\angle 4$ | 5) Substitution Property |
| 6) $m\angle 1 = m\angle 2 + m\angle 3$ | 6) Subtraction Property |

Two Column Proofs - Complete the proof by filling in the blanks.

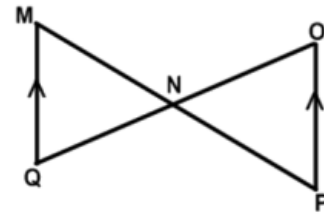
- 1) Given: $GK \parallel HJ$
 Prove: $\triangle GIK \sim \triangle HIJ$



| STATEMENTS | REASONS |
|--|---------------------------------------|
| 1) $GK \parallel HJ$ | 1) Given |
| 2) $\angle K \cong \angle HJI$ | 2) Corresponding angle theorem |
| 3) $\angle G \cong \angle KGH$ | 3) Corresponding Angles |
| 4) $\triangle GIK \sim \triangle HIJ$ | 4) _____ |

2)

Given: $MQ \parallel OP$
 Prove: $\triangle MNQ \sim \triangle PNO$



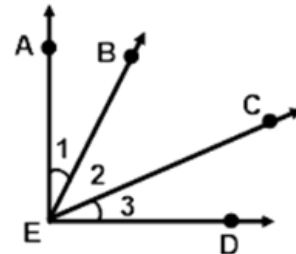
| STATEMENTS | REASONS |
|--|-------------------------------------|
| 1) <u>$MQ \parallel OP$</u> | 1) Given |
| 2) <u>$\angle MNQ \cong \angle ONP$</u> | 2) Vertical Angles |
| 3) $\angle QMN \cong \angle OPN$ | 3) <u>Alternate Interior Angles</u> |
| 4) $\triangle MNQ \sim \triangle PNO$ | 4) <u>AA~</u> |

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Paragraph Proof - Complete the following proof by filling in the blanks.

3)

Given: $m\angle 1 = m\angle 3$
 Prove: $m\angle AEC = m\angle DEB$

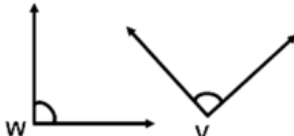


Proof : It is given that $m\angle 1 = m\angle 3$. By the _____ we know that $m\angle 2 = m\angle 2$. So because of the Addition Property we can say, $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 2$. By the Angle Addition Postulate, $m\angle 1 + m\angle 2 = m\angle AEC$. Also, by the Angle Addition Postulate, $m\angle 3 + m\angle 2$ = $m\angle DEB$. By the Transitive Property, $m\angle AEC = m\angle DEB$.

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Complete the proof by filling in the blanks.

4) Given: $\angle W$ and $\angle V$ are congruent and supplementary
 Prove: $\angle W$ and $\angle V$ are right angles

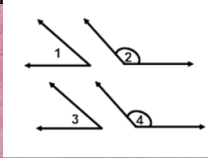


| STATEMENTS | REASONS |
|--|---|
| 1) $\angle W \cong \angle V$ | 1) Given |
| 2) $m\angle W = m\angle V$ | 2) Congruent angles have the same measure |
| 3) $\angle W$ & $\angle V$ are supplementary | 3) Given |
| 4) $m\angle W + m\angle V = 180$ | 4) Definition of supplementary |
| 5) $m\angle W + m\angle W = 180$ or $2m\angle W = 180$ | 5) Substitution Property |
| 6) $m\angle W = 90$ | 6) Division Property |
| 7) $m\angle V = 90$ | 7) Transitive Property |
| 8) $\angle W$ & $\angle V$ are right angles | 8) Definition of right angles |

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Flow Proof - Complete the proof by filling in the blank

5)
 Given: $\angle 1$ and $\angle 2$ are supplementary;
 $\angle 3$ and $\angle 4$ are supplementary;
 $\angle 2 \cong \angle 4$
 Prove: $\angle 1 \cong \angle 3$

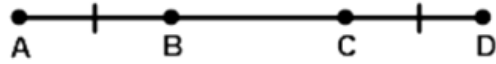


$\angle 1$ and $\angle 2$ are supplementary (Given) $\rightarrow m\angle 1 + m\angle 2 = 180$ (Definition of Supplementary)
 $\angle 3$ and $\angle 4$ are supplementary (Given) $\rightarrow m\angle 3 + m\angle 4 = 180$ (Definition of Supplementary)
 $\angle 2 \cong \angle 4$ (Given) $\rightarrow m\angle 2 = m\angle 4$ (Congruent angles have the same measure)
 $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 4$ (Transitive Property)
 $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 2$ (Substitution Property)
 $\angle 1 \cong \angle 3$ (Subtraction Property)
 $\angle 1 \cong \angle 3$ (Angles with the same measure are congruent)

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Complete the proofs by filling in the blanks.

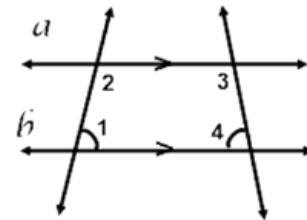
6) Given: $\overline{AB} \cong \overline{CD}$
 Prove: $\overline{AC} \cong \overline{BD}$



| STATEMENTS | REASONS |
|--|--------------------------------------|
| 1) $\overline{AB} \cong \overline{CD}$ | 1) <u>Given</u> |
| 2) $\overline{AB} = \overline{CD}$ | 2) Congruent segments have = length |
| 3) $\overline{BC} = \overline{BC}$ | 3) <u>Reflexive Property</u> |
| 4) $\overline{AB} + \overline{BC} = \overline{BC} + \overline{CD}$ | 4) <u>Addition Property</u> |
| 5) $\overline{AB} + \overline{BC} = \overline{AC}$ | 5) Segment Addition Postulate |
| 6) $\overline{BC} + \overline{CD} = \overline{BD}$ | 6) <u>Segment Addition Postulate</u> |
| 7) <u>$\overline{AC} \cong \overline{BD}$</u> | 7) Substitution Property |

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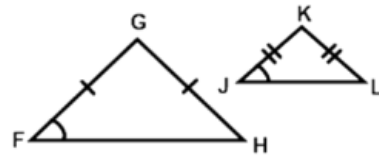
7) Given: $a \parallel b$; $\angle 1 \cong \angle 4$
 Prove: $\angle 2 \cong \angle 3$



| STATEMENTS | REASONS |
|--|--|
| 1) $a \parallel b$ | 1) Given |
| 2) $m\angle 1 + m\angle 2 = 180$ | 2) <u>Consecutive Interior Angles are supplemental</u> |
| 3) $m\angle 3 + m\angle 4 = 180$ | 3) <u>Consecutive Interior Angles are supplemental</u> |
| 4) $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 4$ | 4) <u>Transitive Property</u> |
| 5) <u>$\angle 1 \cong \angle 4$</u> | 5) Given |
| 6) $m\angle 4 + m\angle 2 = m\angle 3 + m\angle 4$ | 6) <u>Substitution Property</u> |
| 7) <u>$m\angle 2 = m\angle 3$</u> | 7) Subtraction Property |
| 8) $m\angle 2 \cong m\angle 3$ | 8) <u>Congruent Angles have = measure</u> |

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8) Given: $FG \cong GH$; $JK \cong KL$; $\angle F \cong \angle J$
 Prove: $\triangle FGH \sim \triangle JKL$

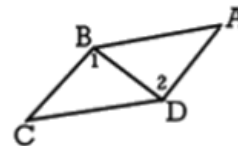


| STATEMENTS | REASONS |
|--|---|
| 1) $FG \cong GH$; $JK \cong KL$ | 1) Given |
| 2) $\triangle FGH$ is isosceles | 2) Definition of isosceles \triangle |
| 3) _____ | 3) Definition of isosceles \triangle |
| 4) $\angle F \cong \angle H$; $\angle J \cong \angle L$ | 4) Base angles of isosceles \triangle are |
| 5) $\angle F \cong \angle J$ | 5) Given |
| 6) $\angle H \cong \angle L$ | 6) Transitive Property |
| 7) $\angle H \cong \angle L$ | 7) Transitive Property |
| 8) $\triangle FGH \sim \triangle JKL$ | 8) AA~ |

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9)

Given: $\overline{AD} \cong \overline{BC}$; $\angle 1 \cong \angle 2$
 Prove: $\triangle ABD \cong \triangle CDB$

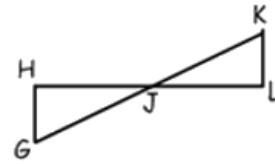


| STATEMENTS | REASONS |
|--|----------|
| 1) $\overline{AD} \cong \overline{BC}$; $\angle 1 \cong \angle 2$ | 1) _____ |
| 2) $\overline{BD} \cong \overline{BD}$ | 2) _____ |
| 3) $\triangle ABD \cong \triangle CDB$ | 3) _____ |

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10)

Given: J is the midpoint of GK
 $\angle H$ and $\angle L$ are right angles
 Prove: $\triangle GHJ \cong \triangle KLJ$



We are given that J is the _____ of GK. Therefore _____ \cong _____.

It is also given that $\angle H$ and $\angle L$ are right angles. Since all right angles are congruent,

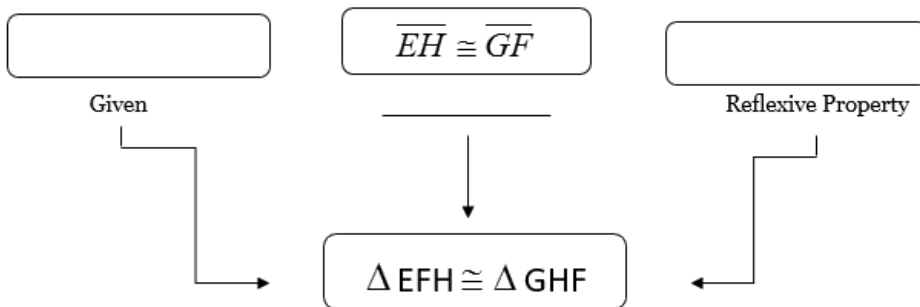
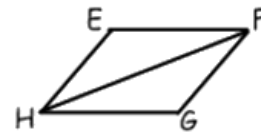
_____ \cong _____. Since _____ and _____ are vertical angles,

_____ \cong _____. Therefore, $\triangle GHJ \cong \triangle KLJ$ by _____.

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11)

Given: $\overline{EF} \cong \overline{GH}$; $\overline{EH} \cong \overline{GF}$
 Proof: $\triangle EFH \cong \triangle GHF$



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Study for Quiz

On-line and textbook help references: p. 44

- <http://www.ixl.com/math/geometry/proofs-involving-parallel-lines>

- <https://www.khanacademy.org/math/geometry/geometry-worked-examples/v/ca-geometry-more-proofs>

- <http://www.regentsprep.org/Regents/math/geometry/GP11/LsimilarProof.htm>

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