



**September 16, 2015**

**Why is the concept of a function important  
and how do I use function notation to show  
variety of situations modeled by functions**

# Today's Standards



**MGSE9-12.F.IF.1.** Understand that a function from one set (called the domain) assigns to each element of the range. If  $f$  is a function and  $x$  is an element of its domain, then  $f(x)$  denotes the output of  $f$  corresponding to the input  $x$ . The graph of  $f$  is the graph of the equation  $y = f(x)$ . *(Draw examples from linear and exponential functions.)*

**MGSE9-12.F.IF.2.** Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. *(Draw examples from linear and exponential functions.)*

# Relation



A relation is any set of ordered pairs.

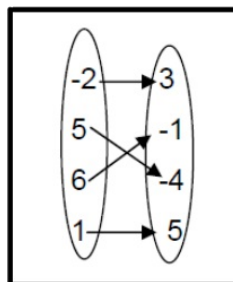
**Examples:**  $\{(1, 4), (-3, 7), (-6, -8)\}$   
 $\{(1, 4), (2, 5), (1, 6)\}$   $\times$

In math a relation can be a table, a mapping or a graph. Think of a relation as "relationship" -- things that are paired together!

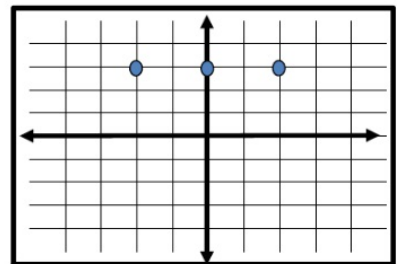
## Table

x	y
2	2
-2	3
0	-1

## Mapping



## Graph



## Everyday examples of a relation

<del>Names of students</del>	Homerooms
<del>Names of U.S. citizens</del>	Social Security #'s

## ↻ Domain and Range of a Relation ↻

**Domain:** the set of all the x-values of a relation

**Range:** the set of all the y-values of a relation

**Example:**  $\{(1, 4), (-3, 7), (-6, -8)\}$

**Domain:**  $\{-6, -3, 1\}$

**Range:**  $\{-8, 4, 7\}$

# Function

A function is a relation where every element of the domain is paired with EXACTLY one element of the range.

## FUNCTION

$\{(1, 4), (-3, 7), (-6, -8)\}$

## NOT A FUNCTION

$\{(1, 4), (2, 5), (1, 6)\}$

# Let's decide what could be a function!



## Example

S:  
1.



F   NF

Reason:

2..



F   NF

Reason:



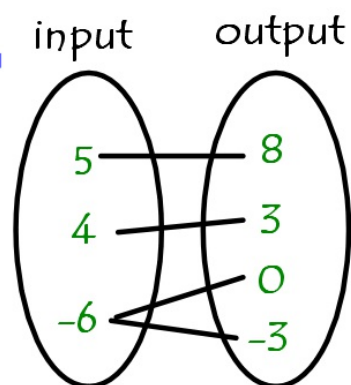
3.

x	y
12	-8
2	3
7	4
-9	4

F   NF

Reason:

4.



F   NF

Reason:

## Input vs. Output

The domain of a function is also called the function's **input**. It gets put "in" to the function.

The range of a function is also called the function's **output**. It is what you get "out" of the function!

REMEMBER: Each input can have ONLY one unique output if the relation is a function!

However, different inputs can have the same output!

**Example:**  $\{(1, 4), (2, 4), (-3, 4)\}$

# Domain & Range

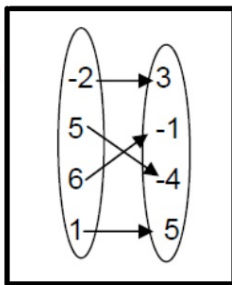
List the domain and range for each of the following.

1.

Domain:  $\{-8, -4, 2, 5\}$   
Range:  $\{-2, 3, 5\}$



2.



Domain:  $\{-2, 5, 6, 1\}$   
Range:  $\{-4, -1, 3, 5\}$

3.

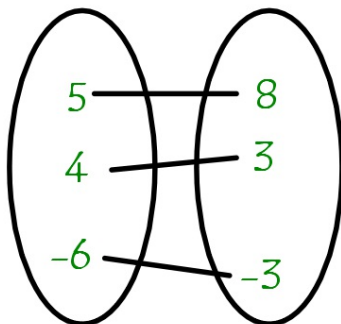
x	y
12	-8
2	3
7	4
-9	4

Domain:  $\{-9, 2, 7, 12\}$   
Range:  $\{-8, 3, 4\}$



4.

input      output



Domain:  $\{-6, 4, 5\}$   
Range:  $\{-3, 3, 8\}$



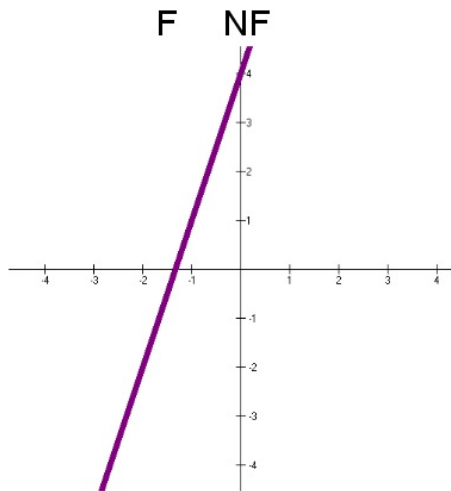




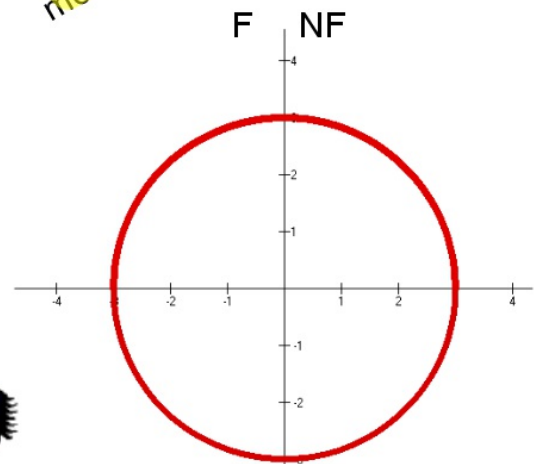
# Now let's look at the Vertical Line Test (VLT)

The vertical line test for functions states that a graph is a function if any vertical line intersects the graph at no more than **one point** (at a particular time).

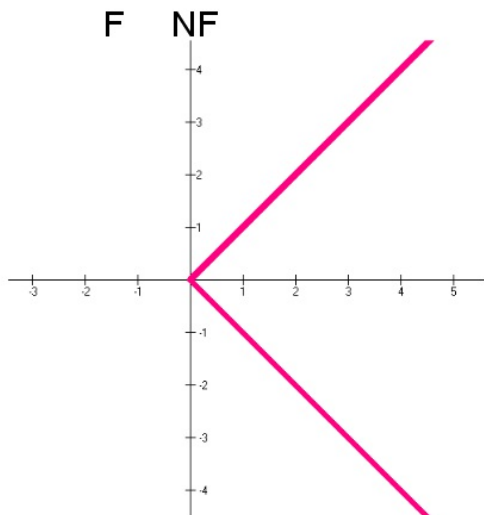
5.



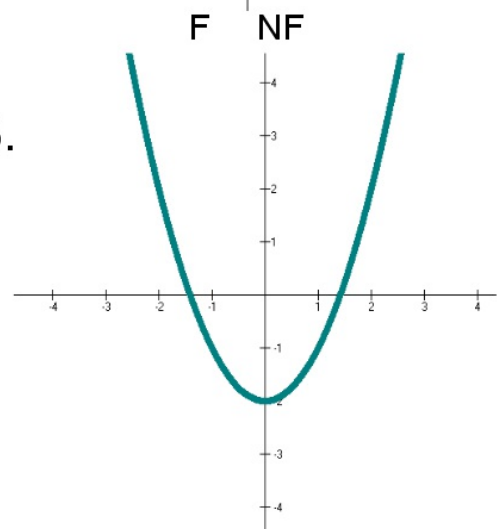
6.



7.



8.



# Function Notation



Click the star!



$f(x)$  is read "f of x"



$$y = 2^x$$



$$g(x) = 2^x$$

$g(x)$  is read "g of x"

Functions do not always use the letter  $f$ .

Any letter can be used but  $f$  and  $g$  are used most often when dealing with functions.

Write the following equations in  
function notation.

1.  $y = -6x - 2$

$f(x) = -6x - 2$

2.  $y = 4x + 1$

$g(x) = 4x + 1$

3.  $y = \frac{2}{3}x - 7$

$g(x) = \frac{2}{3}x - 7$

4.  $y = 123 + \frac{7}{8}x$

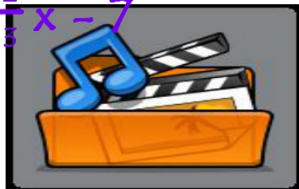
$f(x) = 123 + \frac{7}{8}x$

5.  $y = 5^x$

$f(x) = 5^x$

6.  $y = x^2 - 4$

$g(x) = x^2 - 4$



# Homework



**Complete  
Practice Handout**

