

Analytic Geometry

March 17, 2016

Inscribed and Circumscribed Angles.

EQ: How is the central angle of a circle and an inscribed angle related?

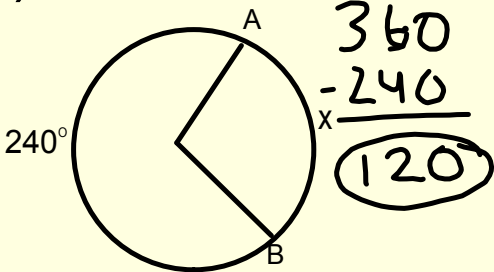
MCC9-12.G.C.2 Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles, the radius of a circle is perpendicular to the tangent where the radius intersects the circle.

Quiz:

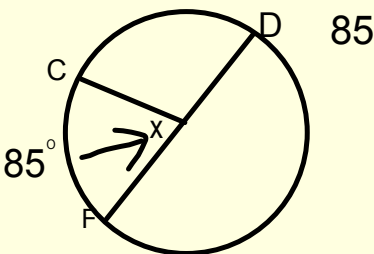
Circle Vocabulary

Warm-up

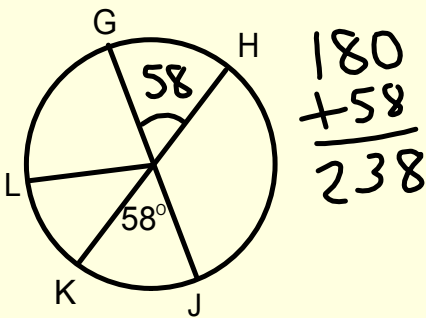
1) Find x



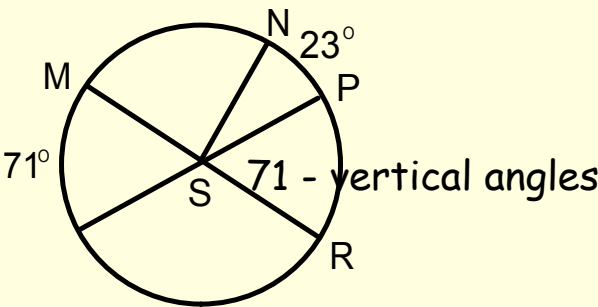
2) Find x



3) Find arcGHK



4)



Homework Answers

1) 120°

2) 123°

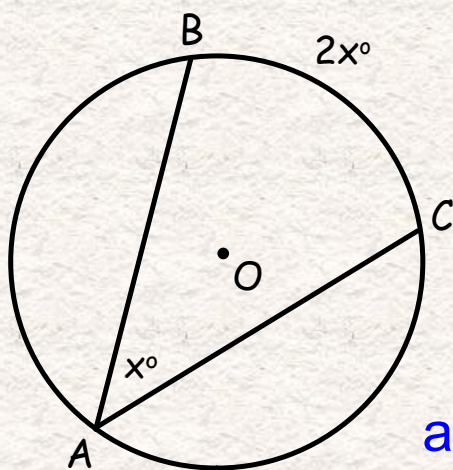
3) 306°

4) 234°

5) 125°

6) 8

Inscribed Angles



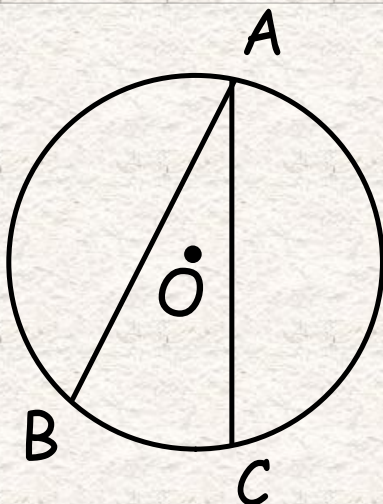
Properties of Inscribed Angles

- vertex lies on the circle
- sides are chords of the circle.
- corresponding arc is equal to twice the measure of the inscribed angle.

$$\text{arc} = 2(\text{angle}) \quad \text{or} \quad \text{angle} = \frac{\text{arc}}{2}$$

Let's Practice

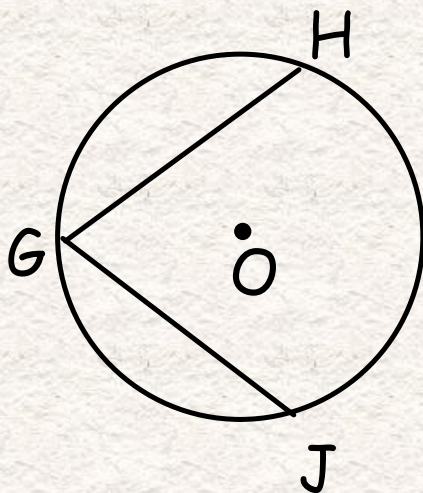
1)



If $\angle BAC = 31^\circ$,

$$m\widehat{BC} = ? \quad 62$$

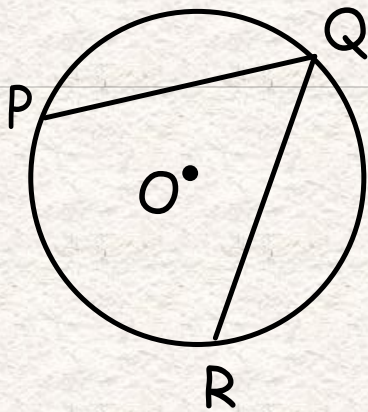
2)



If $\angle HGJ = 84^\circ$,

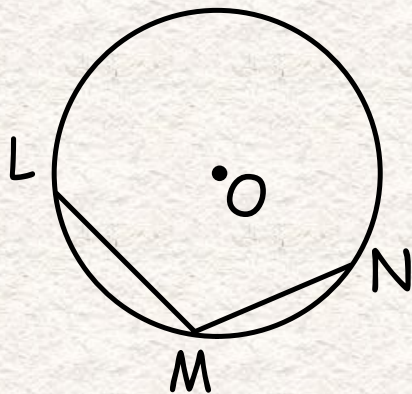
$$m\widehat{HJ} = ? \quad 168$$

3)



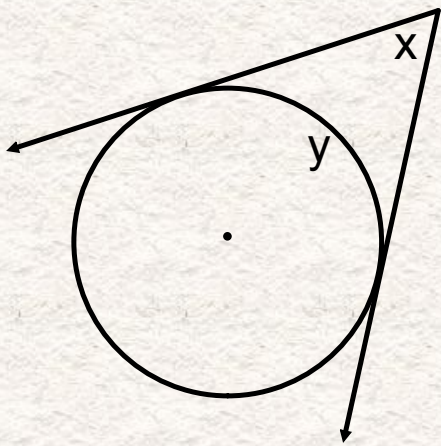
If $m\widehat{PR} = 160^\circ$
 $\angle PQR = ?$ 80

4)



If $m\widehat{LN} = 240^\circ$
 $\angle LMN = ?$ 120

Circumscribed Angles



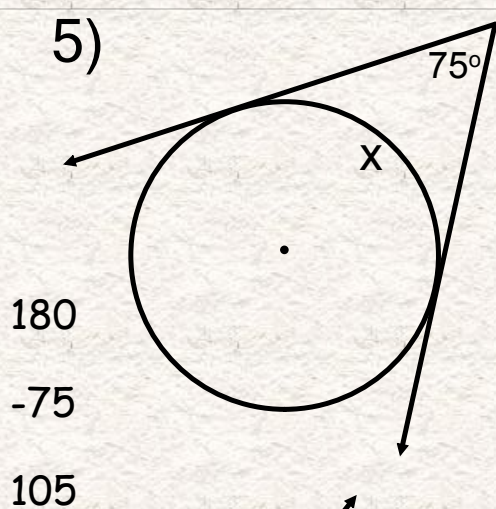
Properties of Circumscribed Angles

- vertex lies outside of the circle.
- sides are tangents of the circle.
- circumscribed angle and corresponding arc sum to 180° .

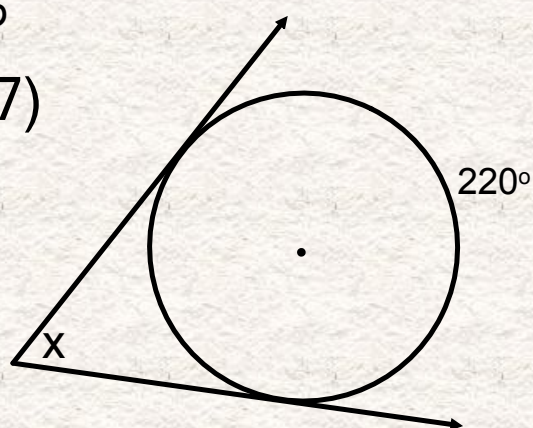
$$x + y = 180^\circ$$

Let's Practice

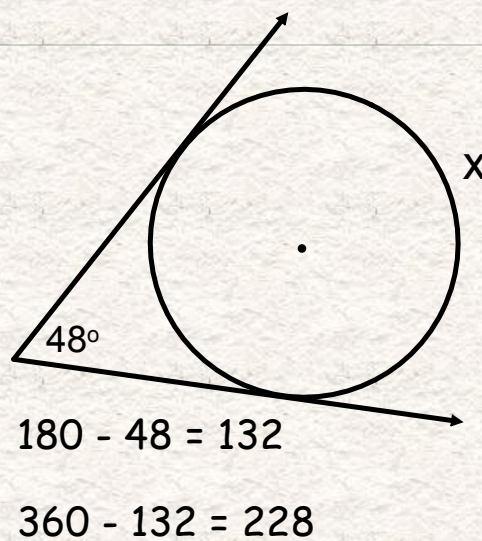
5)



7)



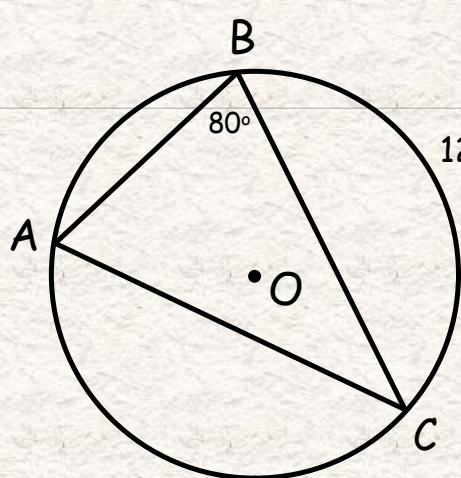
6)



$$360 - 220 = 140$$

$$140/2 = 70$$

$$x=70$$



$\triangle ABC$ is inscribed in circle O .
 $\angle ABC = 80^\circ$ and $\widehat{AC} = 120^\circ$

Find the measures of:

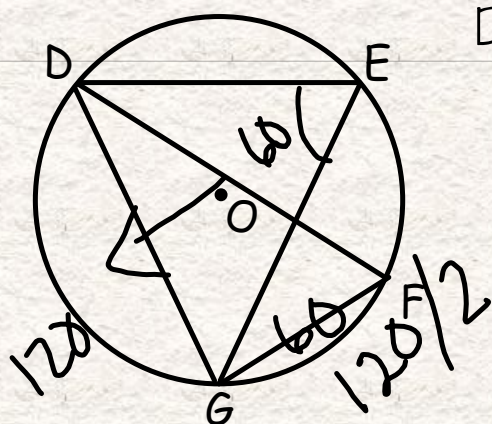
$$\angle BAC = 360 - 120 = 240$$

$$\angle ACB = 80 \times 2 = 160$$

$$160 + 120 = 280$$

$$\widehat{AB} = 360 - 280 = 80$$

$$\widehat{AC} = 80 \times 2 = 160$$



$\triangle DGE$ is an equilateral triangle
 \overline{DF} bisects $\angle EDG$.

Find the measure of:

$\angle DEG = 180 / 3 = 60$ for each
 angle.

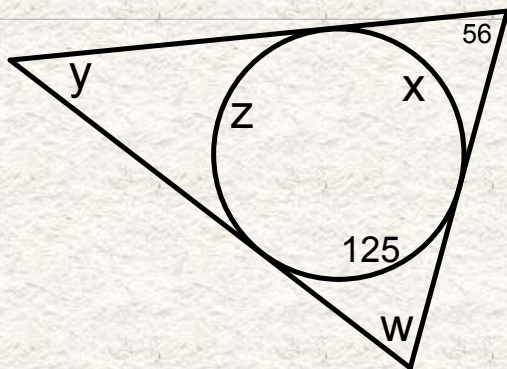
$$\widehat{DG} = 60 \times 2 = 120$$

$$\widehat{FE} = 60 \times 2 = 120$$

$$120 / 2 \text{ (bisector)} = 60$$

$$\angle DGF = 180$$

Find the missing measures.



$$w = (180 - 125) = 55$$

$$x = (180 - 56) = 124$$

$$y = 180 - (55 + 56) = 69$$

$$z = 180 - 69 = 111$$

HW: Worksheet

On-line and textbook help references: pp. 209 - 518

- <https://learnzillion.com/lessons/3249-find-relationships-between-central-and-circumscribed-angles>
- <https://www.khanacademy.org/math/geometry/cc-geometry-circles/central-inscribed-circumscribed/e/central--inscribed--and-circumscribed-angles>
- <http://www.cliffsnotes.com/math/geometry/circles/arcs-and-inscribed-angles>